

# Chromatography (I)

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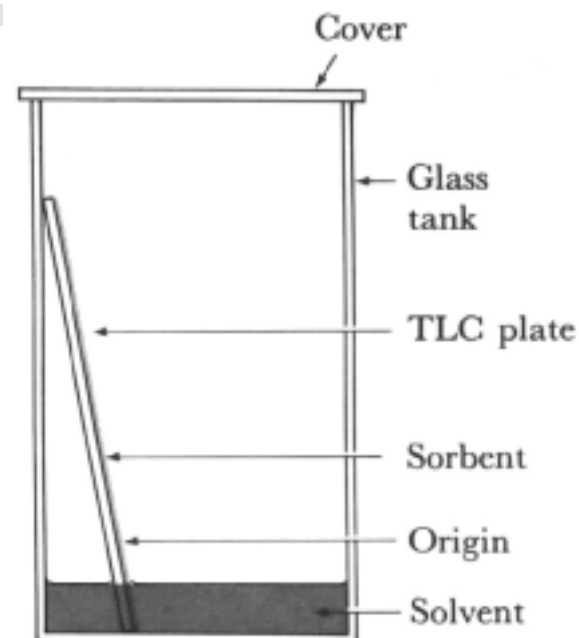
# Objectives

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- The **physical basis** of chromatography
- The **chemical basis** of the principal chromatography methods
- **Performance criteria** for comparing chromatography systems

# History

- 1903 Mikhail Tswett (Russian)
  - Separate plant pigments
  - "chroma" – color in greek
  - Example
    - Thin layer chromatography (TLC)
- Chromatography
  - A separation technique
  - Based on the different **adsorptive** or **partitioning** properties of the sample molecules.



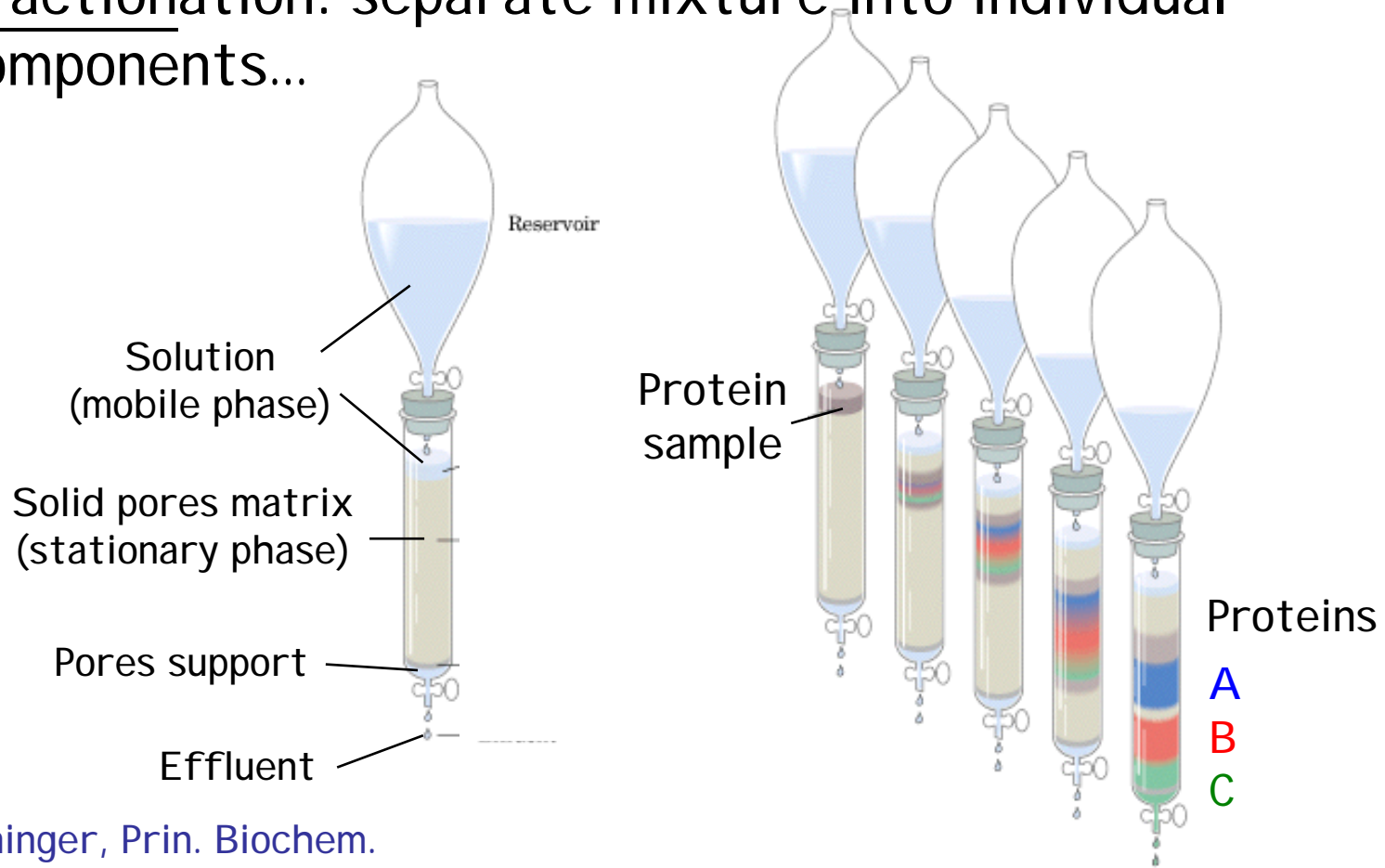
# Basic principle

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- Chromatography system
  - Stationary phase
    - The stationary adsorbant (immobilized)
  - Mobile phase
    - The fluid moving through the chromatographic column
- Molecule partition between two phases
  - Partition coefficient,  $K_d$ 
    - $K_d = C_s / C_m$ 
      - C = [sample] in the S and M phases
      - K is affected by temperature, solvent polarity, etc.
- Separate a mixture into its components

# Column Chromatography

- Stationary phase + mobile phase
- By **charge, size, binding affinity** difference
- Fractionation: separate mixture into individual components...



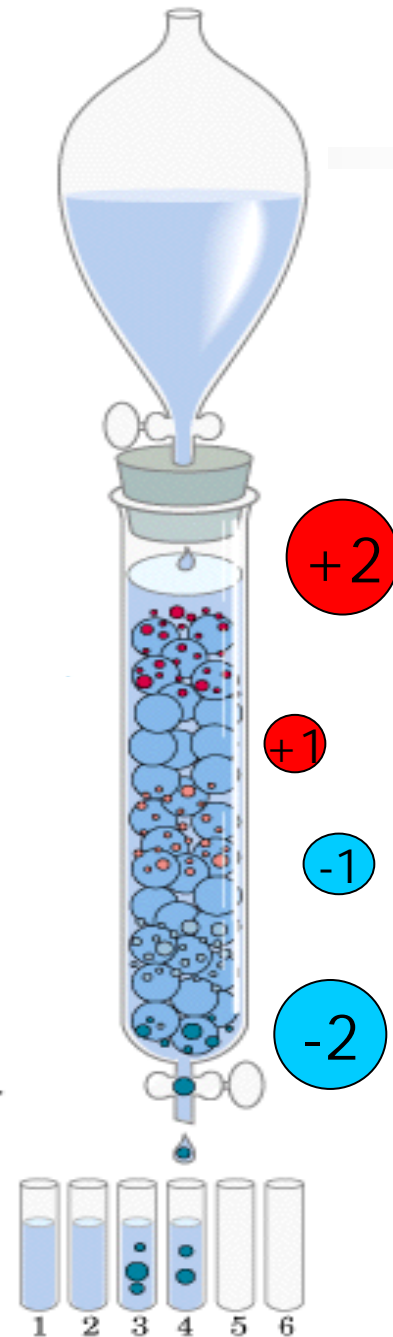
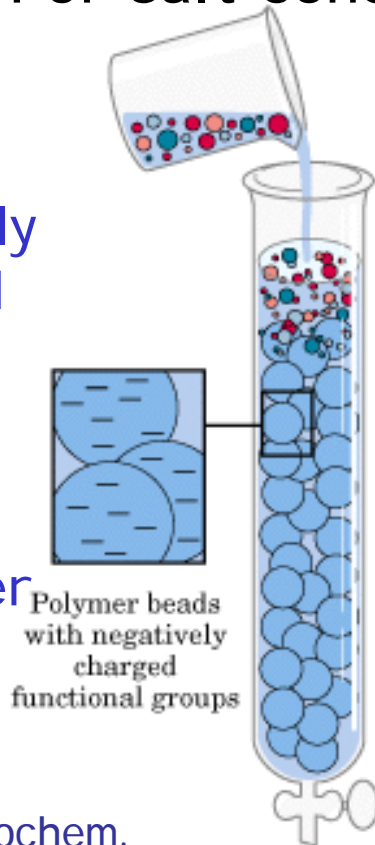
# I on Exchange

- By charge difference
- Cation and anion exchanger
  - Refers to the target interested
- Changing pH or salt concentration

Negatively  
charged  
beads

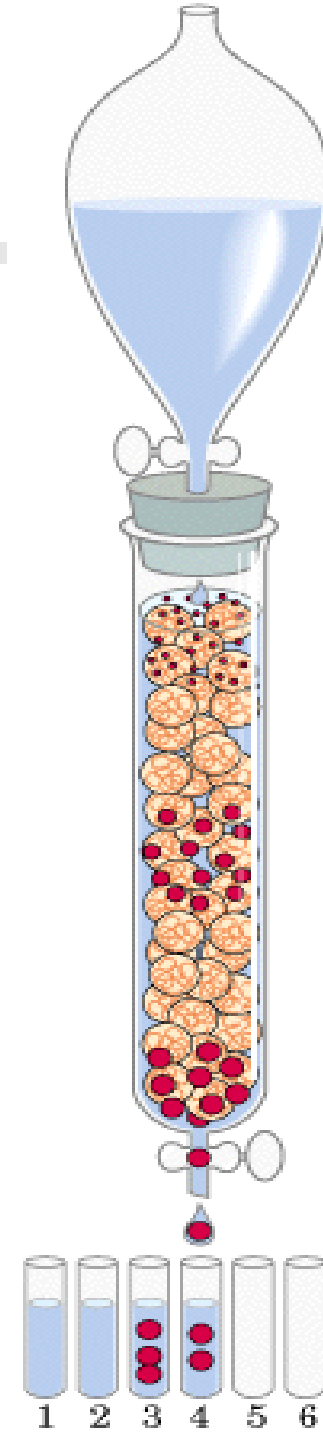
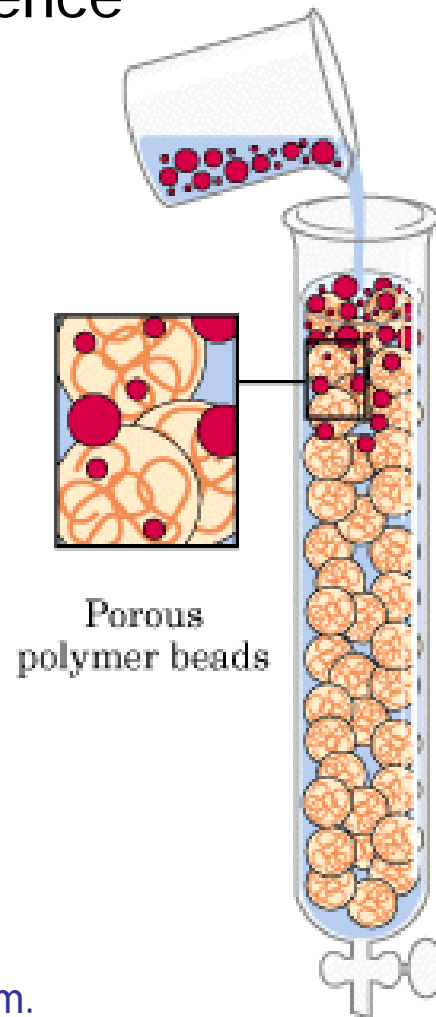
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Cation  
exchanger



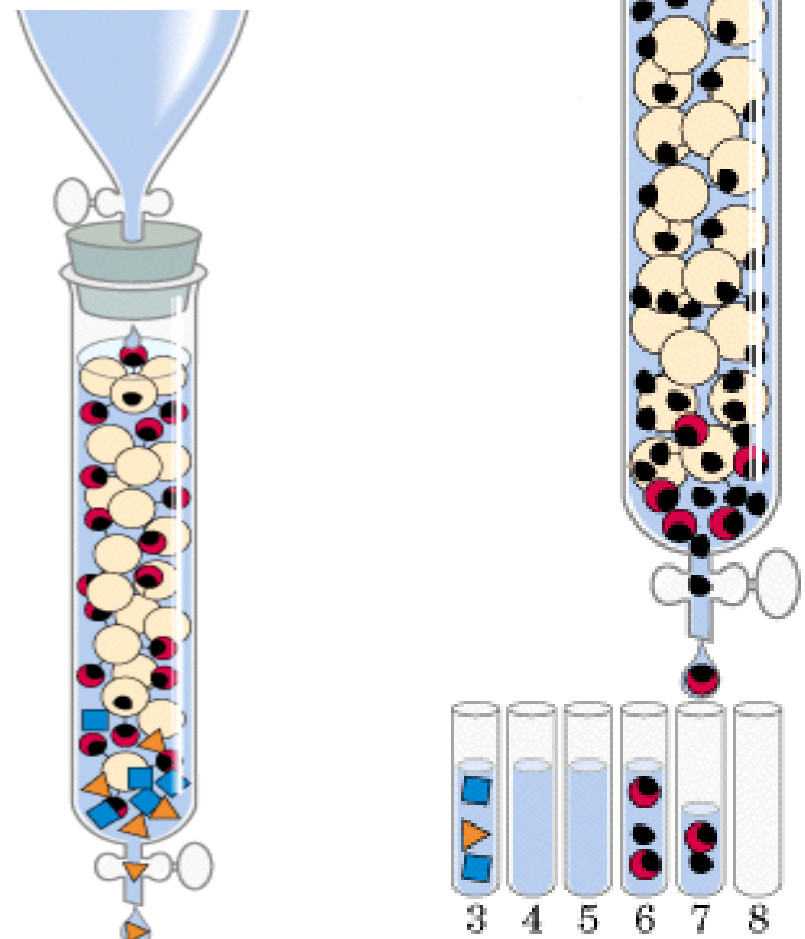
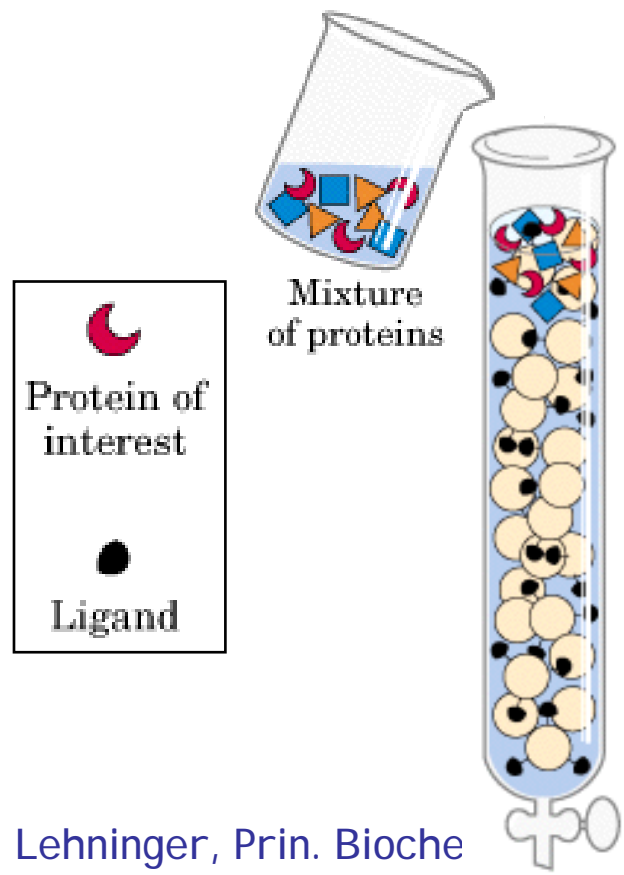
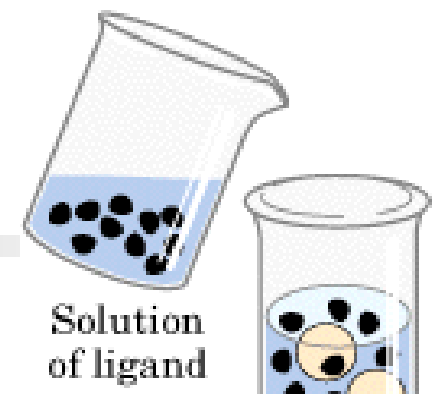
# Gel filtration

- Size-exclusion, gel permeation
- By **size** difference
- Pores beads



# Affinity

- By protein-ligand binding specificity
  - His-tag fusion protein and Ni-column
  - GST-fusion protein and GSH-column





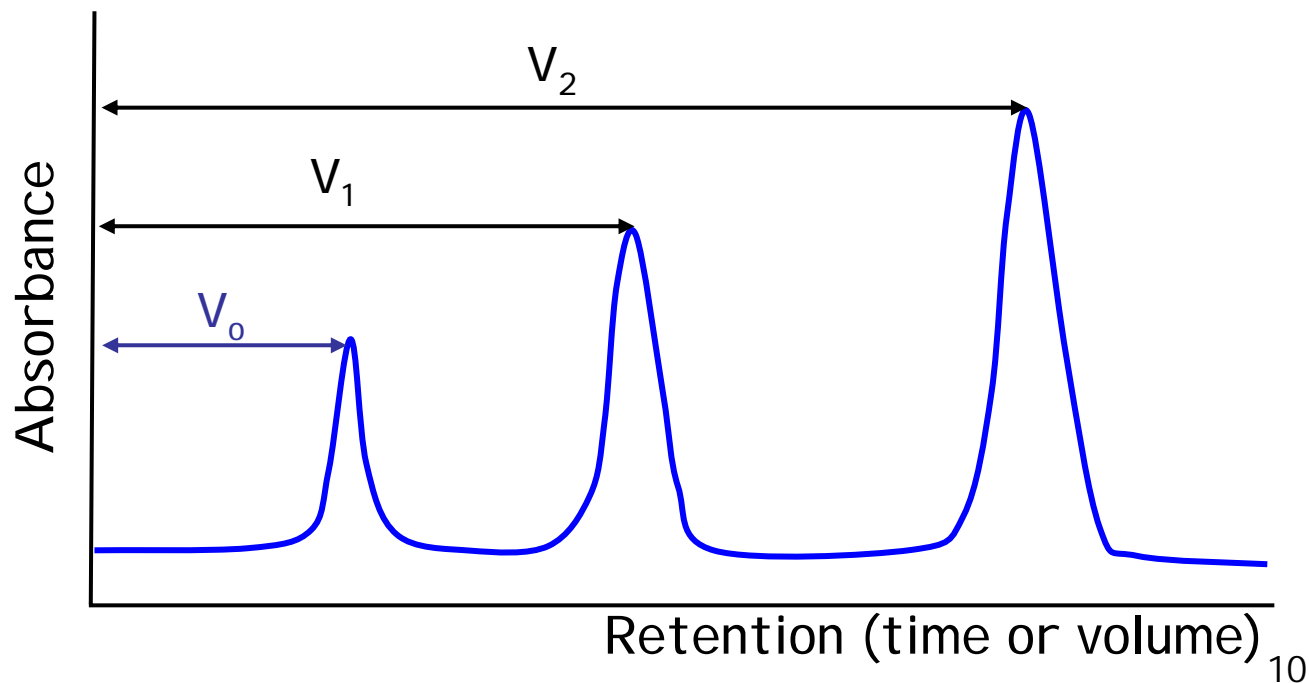
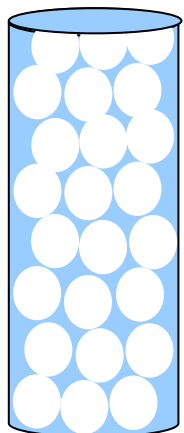
# Performance parameters

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- For comparison of different systems:
  - Retention
  - Resolution
  - Peak broadening
  - Plate number
  - Peak symmetry
  - Capacity factor

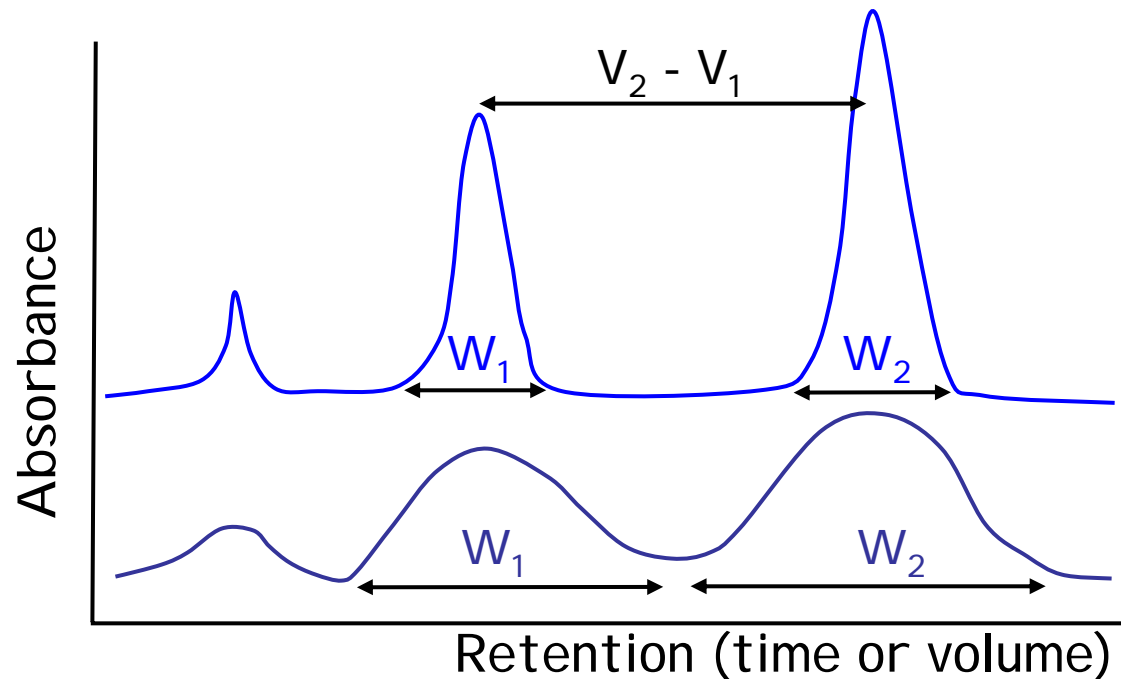
# Retention

- Samples are retained on column to different extent
  - Retention time ( $t_R$ ), retention volume ( $V_R$ )
    - $V_R = f t_R$ ,  $f$  = flow rate
    - Retention  $\propto$  column length,  $1/f$
  - Void (excluded) volume,  $V_0$ 
    - The contained volume of the column - volume of packed matrix



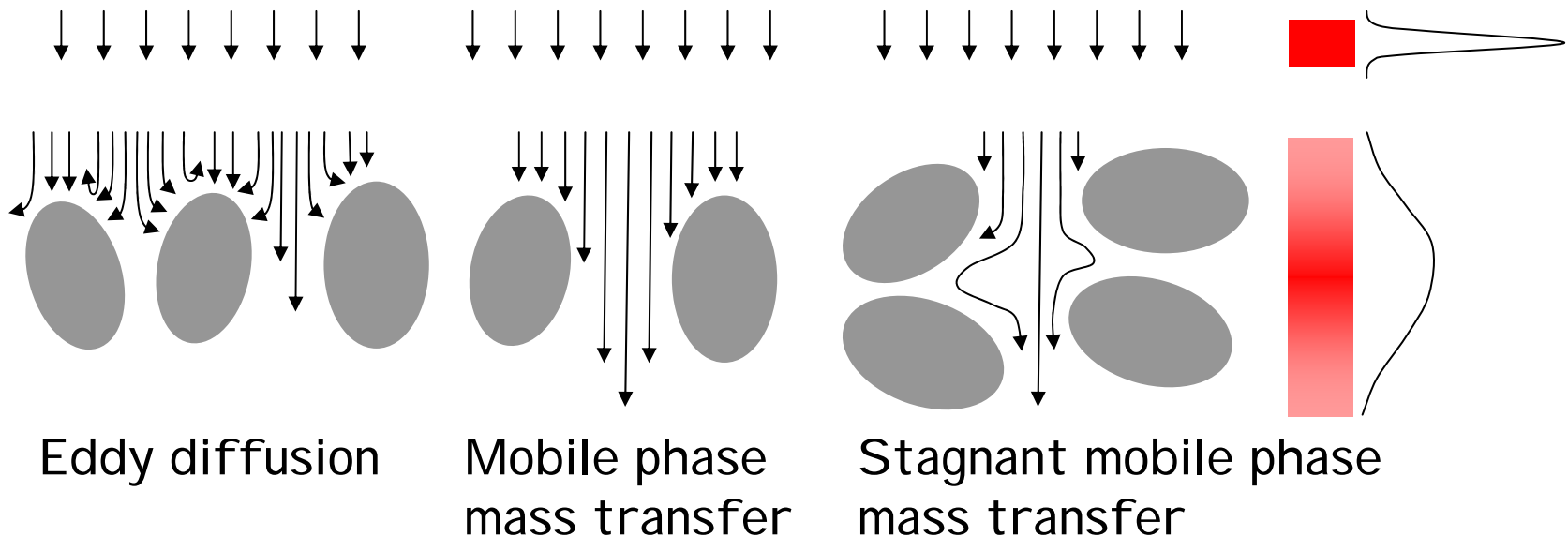
# Resolution (R)

- Describe how well peaks are separated
  - $R = (V_2 - V_1) / \frac{1}{2} (W_1 + W_2)$ 
    - Well separated (large  $V_2 - V_1$ )
    - Narrow peaks (small  $W$ )



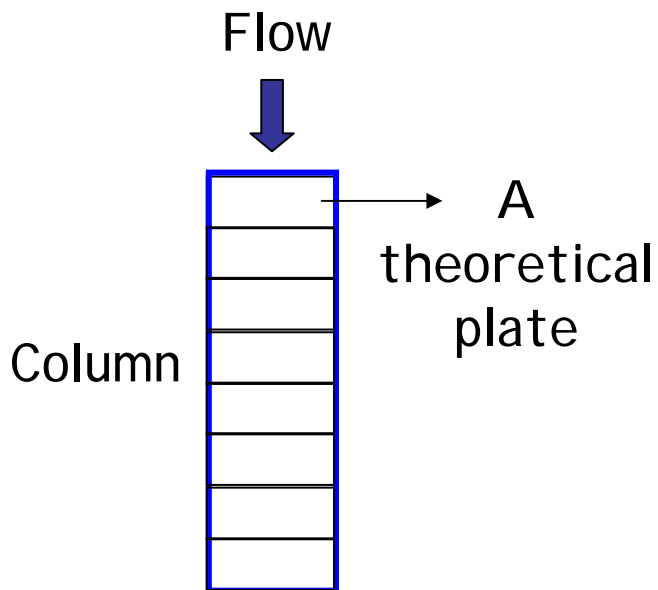
# Peak broadening

- Eluted volume > applied sample volume
  - Diffusion
    - Sample interact with stationary phase
  - Mass transfer phenomena
    - Within mobile and/or stationary phase



# Theoretical plates

- The column is made of very thin, horizontal plates
  - A very thin section within which molecules can partition between mobile and stationary phases.



When  $K_d = 1$ , total of 256 molecules in the sample:

## One plate

	Stationary phase	Mobile phase
Plate 1	128	128



## Two plates

Plate 1	64	64
Plate 2	64	64

# Partition between phases

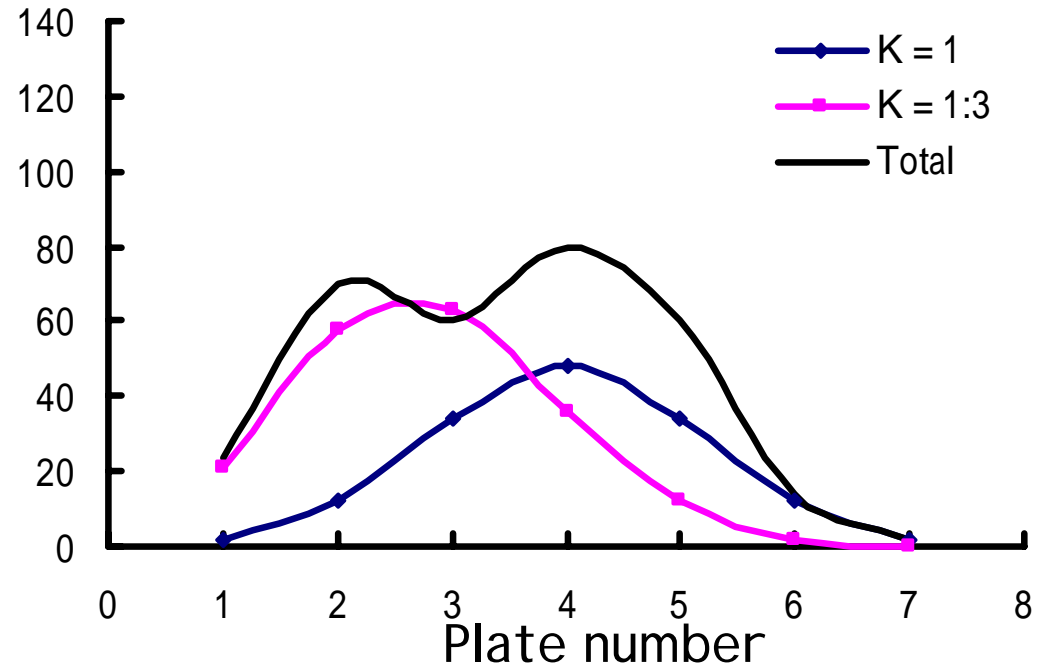
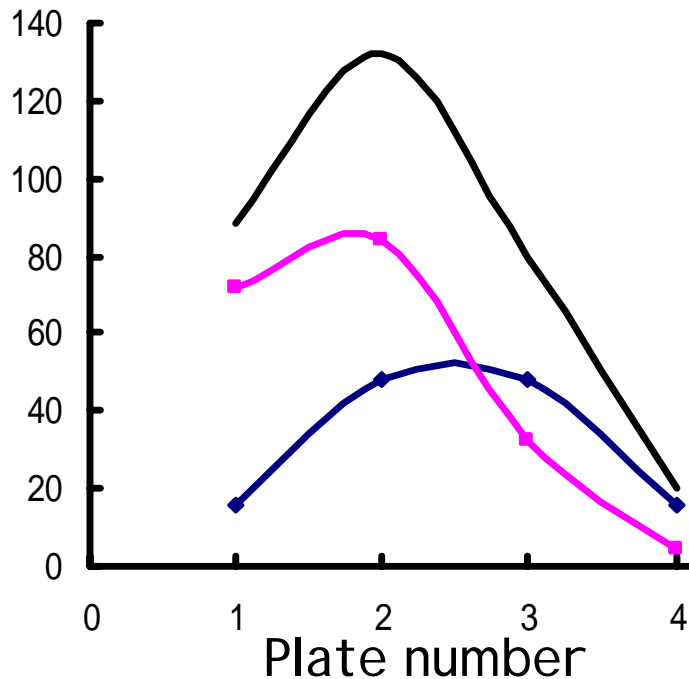
- Redistribution of the molecules between the stationary and mobile phase

When  $K_d = 1$ , total of 128 molecules in the mobile

phase	N=1	N=2	N=3	N=4	N=5	N=6	N=7	N=8
Plate 1	128	64	32	16	8	4	2	1
Plate 2		64	64	48	32	20	12	6
Plate 3			32	48	48	48	34	23
Plate 4				16	32	48	48	41
Plate 5					8	20	34	41
Plate 6						4	12	23
Plate 7							2	6
Plate 8								1

# Good resolution

- Large plate number and small plate height
  - Plate number (N)
    - The column is made of very thin, horizontal plates
  - Plate height (H)
    - $H = \text{column length}/N$

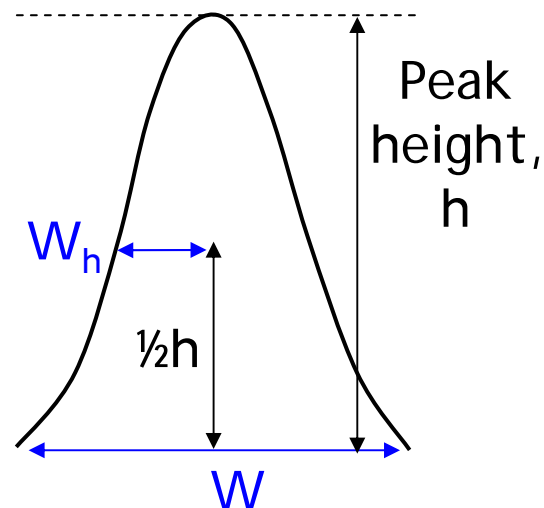


# Theoretical plate number, N

- Related to the surface area of the particles of which the stationary phase is composed

$$N = 16 \left( \frac{t_R}{W} \right)^2$$

$$\text{or } N = 5.54 \left( \frac{t_R}{W_h} \right)^2$$

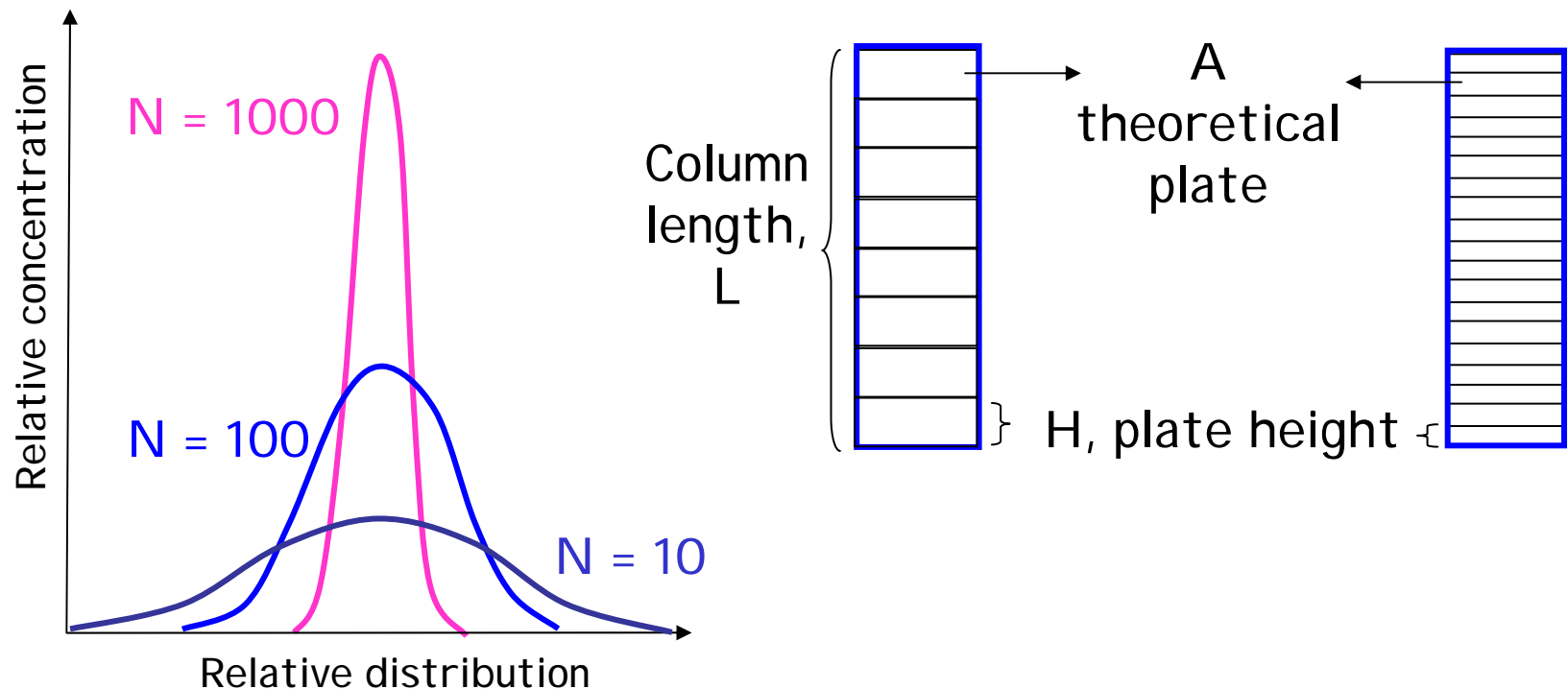


- Two columns of different length (e.g. 15 and 30 cm) containing the same number of theoretical plates (e.g. a typical 15 x 0.46 cm C-8 reverse phase column has  $N \sim 13000$ ). **Which one has better chromatographic performance ?**



# Plate height number, H

- Height equivalent to a theoretical plate (HETP)
  - $H = L/N$
- Broadening (W) is correlated with the plate number (N)
  - Large N and small H, small W
  - Small N and large H, large W

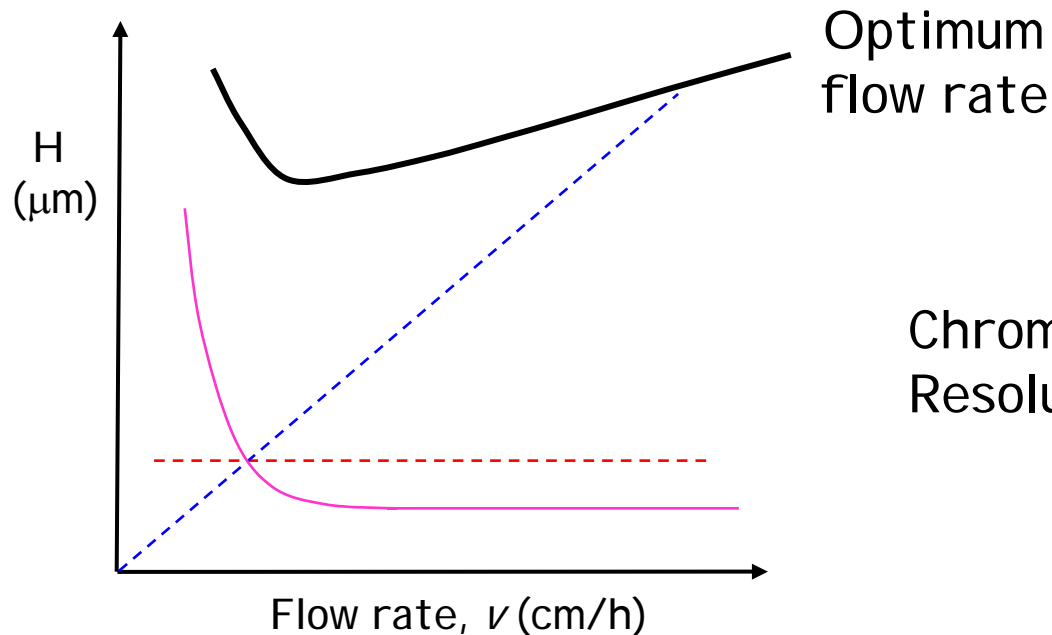


# Broadening again...

- $W \propto H$ 
  - Causes of broadening (in terms of  $H$ )
    - Eddy diffusion:  $H_1 = C_e d_p$
    - Mobile phase mass transfer:  $H_2 = C_m d_p^2 \nu / D_m$
    - Stagnant mobile phase MT:  $H_3 = C_{sm} d_p^2 \nu / D_m$ 
      - $C$ : coefficients for the particular **class of particle** used as stationary phase
      - $d_p$ : particle diameter
      - $\nu$ : flow rate of mobile phase
      - $D_m, D_s$ : diffusion coefficients of a sample in the mobile and stationary phase
  - $H = H_1 + H_2 + H_3$
  - $H = C_e d_p + C_m d_p^2 \nu / D_m + C_{sm} d_p^2 \nu / D_m$
- **To reduce broadening (small  $W$ ), choose...**
  - **Particle type** (material)
  - **Small  $d_p$**  (particle diameter)
  - **Small  $\nu$**  (flow rate of mobile phase)
  - **Large  $D_m, D_s$**  (diffusion coefficients of a sample)

# Optimum flow rate

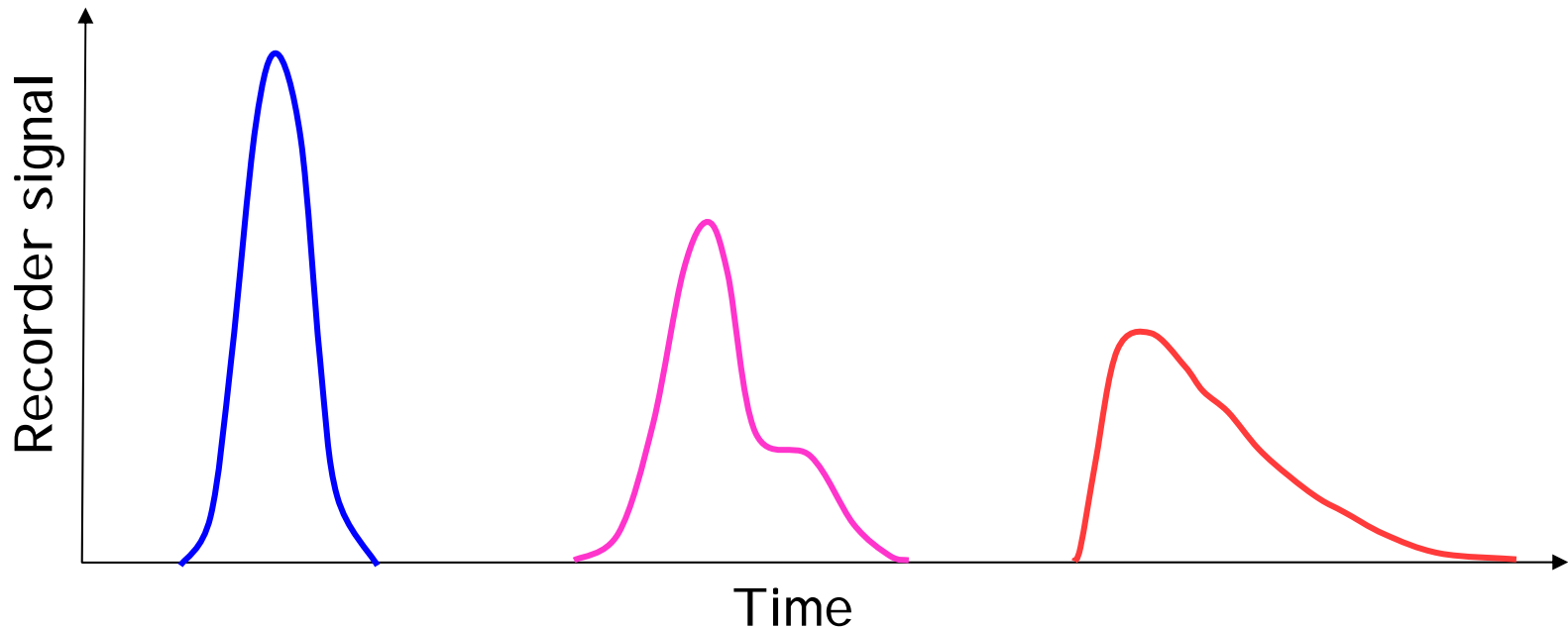
- The van Deemter curve
  - A plot of H versus the flow rate ( $v$ )
  - $H = A + B/v + C_v$ 
    - A: Eddy diffusion
    - B: longitudinal diffusion (along the direction of flow)
    - C: the mass transfer effect



Chromatography efficiency:  
Resolution vs. Analysis time

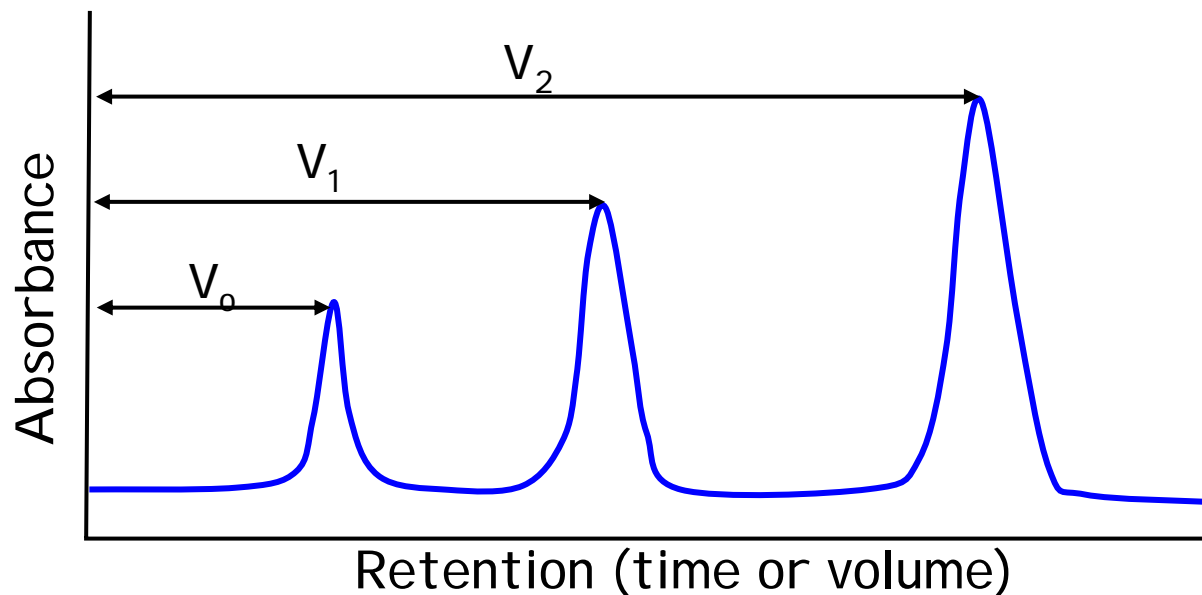
# Peak symmetry

- **Gaussian shape** (normal distribution)
  - Cause of distortion
    - Non-linear flow rates
    - Incomplete separation of peaks (shoulder)
    - Trailing



# Capacity (retention) factor, $k$

- For each component in the sample
  - $k_1 = (V_1 - V_0)/V_0$ ,  $V_0$  = void volume
  - or  $k_1 = (t_1 - t_0)/t_0$ ,  $t_0$  = dead time
  - $k = K_d (V_s/V_m)$ ,  $V$  = volume of stationary or mobile phase
- Separation (selectivity) factor,  $\alpha$ 
  - $\alpha = k_2/k_1$ 
    - $\alpha \geq 1$ , species 1 elutes faster than species 2



# Exercise 1

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- Calculate the capacity factor ( $k$ ) for an analyte in a column in which the volume of the stationary phase is one-fifth of that of the mobile phase if:
  - 1)  $k$  (partition coefficient) = 1
  - 2)  $k$  (partition coefficient) = 50

# Exercise 2

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- An analyte eluted from a chromatographic column as a Gaussian peak with a retention time of 7 min 45 sec and a base peak width of 30 sec.
- Calculate:
  - 1) The number of theoretical plates in the column;
  - 2) The plate height if the column was 7.5 cm long.

# Exercise 3

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- Two compounds (1 and 2) with distribution coefficients of 10 and 12 are to be separated on a column in which the volume of the stationary phase is one-fifth that of the mobile phase.
- Calculate
  - The number of theoretical plates required to give a resolution of 1.5.



# Exercise 4

- Two compounds A and B were separated on a 25 cm long column. The observed retention times were 7 min 20s and 8 min 20s, respectively. The base peak width for analyte B was 10s.
- When a reference compound, which was completely excluded from the stationary phase under the same elution conditions, was studied, its retention time was 1 min 20s.
- Calculate
  - 1) The adjusted retention time for A and B;
  - 2) The capacity factor for A and B;
  - 3) The selectivity factor for the two compounds;
  - 4) The number of theoretical plates in the column;
  - 5) The resolution of the two compounds;
  - 6) The required column length to double the resolution.